## DE2 Electronics 2

## Tutorial Sheet 3 - Laplace Transform and Transfer Functions

> (Lectures 6-7)

* indicates level of difficulty
1.* By direct integration or table look up, find the one-sided Laplace transforms of the following functions:
a) $\quad u(t)-u(t-1)$
b) $t e^{-t} u(t)$
c) $\quad t \cos \omega_{0} t u(t)$.
2.* By direct integration or otherwise, find the Laplace transforms of the following signals:

(a)

(b)
3.* Find the inverse (one-sided) Laplace transforms of the following functions:
a) $\frac{2 s+5}{s^{2}+5 s+6}$
b) $\frac{(s+1)^{2}}{s^{2}-s-6}$
4.** Find the Laplace transforms of the following function using the Laplace Transform Table and the time-shifting property where appropriate.
a) $u(t)-u(t-1)$
b) $\quad e^{-(t-\tau)} u(t)$
c) $\quad \sin \left[\omega_{0}(t-\tau)\right] u(t-\tau)$
5.** For each of the system described by the following differential equations, find the system transfer function.
a) $\frac{d^{2} y}{d t^{2}}+11 \frac{d y}{d t}+24 y(t)=5 \frac{d f}{d t}+3 f(t)$
b) $\frac{d^{3} y}{d t^{3}}+6 \frac{d^{2} y}{d t^{2}}-11 \frac{d y}{d t}+6 y(t)=3 \frac{d^{2} f}{d t^{2}}+7 \frac{d f}{d t}+5 f(t)$

